Important Concepts not on the AP Statistics Formula Sheet

Part I:	portant Concepts not on the AF	Statistics Formula Shee	t
IQR = $Q_3 - Q_1$ Test for an outlier:1.5(IQR) above Q_3 or below Q_1 The calculator will run thetest for you as long as youchoose the boxplot with theoulier on it in STATPLOT	Linear transformation: Addition : affects center NOT spread adds to \bar{x} , M, Q ₁ , Q ₃ , IQR not σ Multiplication: affects both center and spread multiplies \bar{x} , M, Q ₁ , Q ₃ , IQR, σ	When describing data: describe center, spread, and shape. Give a 5 number summary or mean and standard deviation when necessary.	Histogram: fairly symmetrical unimodal
skewed	Skewed left	Ogive (cumulative	Boxplot (with an
right 20 20 15 10 10 10 1 2 3 4 5 6 7 8 9 10 11 12		frequency) 100 - 100	outlier)
Number of letters in word Stem and leaf	Normal Probability Plot	(b) Age at inauguration $x - mean$	r: correlation coefficient,
Treasury bills 0 9 1 02556668 2 15779 3 011355899	140- 130- 170-	$z = \frac{1}{\text{standard dev}}$ $z = \frac{\sigma r}{\sigma}$	The strength of the linear relationship of data. Close to 1 or -1 is very close to linear
4 24778 5 112225667879 6 24569 7 278 8 048 9 8 10 45 11 3 12 13 14 7 (b)	The 80 th percentile means that 80% of the data is below that observation.	HOW MANY STANDARD DEVIATIONS AN OBSERVATION IS FROM THE MEAN 68-95-99.7 Rule for Normality N(μ,σ) N(0,1) Standard Normal	 r²: coefficient of determination. How well the model fits the data. Close to 1 is a good fit. "Percent of variation in y described by the LSRL on x"
residual = $y - \hat{y}$ residual = observed – predicted	Exponential Model: y = ab ^x take log of y Power Model: y = ax ^b take log of x and y	Explanatory variables explain changes in response variables. EV: x, independent RV: y, dependent	Lurking Variable: A variable that may influence the relationship bewteen two variables. LV is not among the EV's
y = a+bx Slope of LSRL(b): rate of change in y for every unit x	y an une log of k une y	itti y, dependent	
y-intercept of LSRL(a): y when $x = 0$			
Confounding: two variables are confounded when the effects of an RV cannot be distinguished.	$(x) \longrightarrow (y)$		
	Causation (a)	Common response (b)	Confounding (c)

Regression in a Nutshell

Given a Set of Data:

a second s								
NEA change (cal):	-94	-57	-29	135	143	151	245	355
Fat gain (kg):	4.2	3.0	3.7	2.7	3.2	3.6	2.4	1.3
NEA change (cal):	392	473	486	535	571	580	620	690
Fat gain (kg):	3.8	1.7	1.6	2.2	1.0	0.4	2.3	1.1

Enter Data into L₁ and L₂ and run 8:Linreg(a+bx)

The regression equation is:

predicted fat gain = 3.5051 - 0.00344(*NEA*)

y-intercept: Predicted fat gain is 3.5051 kilograms when NEA is zero.

slope: Predicted fat gain decreases by .00344 for every unit increase in NEA.

r: correlation coefficient

r = -0.778Moderate, negative correlation between NEA and fat gain.

r²: coefficient of determination

 $r^2 = 0.606$

60.6% of the variation in fat gained is explained by the Least Squares Regression line on NEA. The linear model is a moderate/reasonable fit to the data. It is not strong.

The residual plot shows that the model is a reasonable fit; there is not a bend or curve, There is approximately the same amount of points above and below the line. There is No fan shape to the plot. 3+

Predict the fat gain that corresponds to a NEA of 600.

predicted fat gain = 3.5051 - 0.00344(600)predicted fat gain = 1.4411

Would you be willing to predict the fat gain of a person with NEA of 1000?

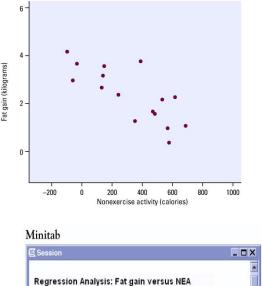
No, this is extrapolation, it is outside the range of our data set.

Residual: observed y - predicted y

Find the residual for an NEA of 473

First find the predicted value of 473:

predicted fat gain = 3.5051 - 0.00344(473)predicted fat gain = 1.87798



SE Coef

-0.0034415 0.0007414 -4.64 0.000

0.3036 11.54 0.000

The regression equation is Fat gain = 3.51 - 0.00344 NEA

Coef

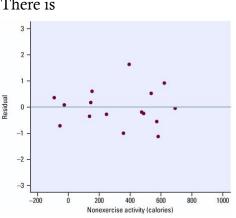
S = 0.739853 R-Sg = 60.6% R-Sg(adj) = 57.8%

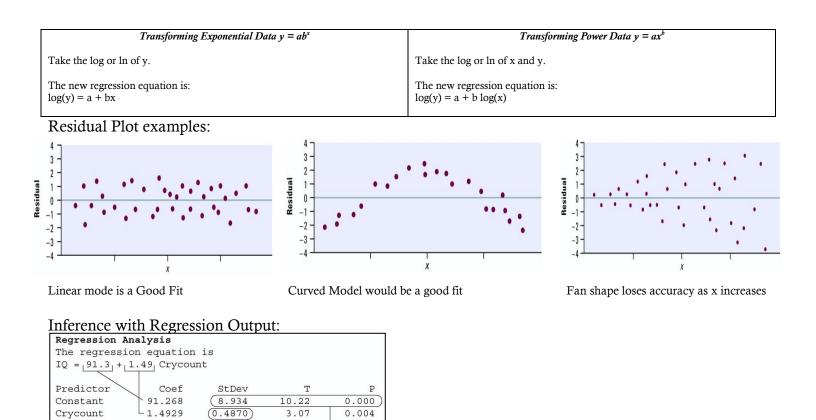
3.5051

Predictor

Constant

NEA





Construct a 95% Confidence interval for the slope of the LSRL of IQ on cry count for the 20 babies in the study.

Formula: df = n - 2 = 20 - 2 = 18 $b \pm t^*SE_b$ $1.4929 \pm (2.101)(0.4870)$ 1.4929 ± 1.0232 (0.4697, 2.5161)

Find the t-test statistic and p-value for the effect cry count has on IQ.

SE,

We usually

ignore this part.

From the regression analysis t = 3.07 and p = 0.004

R-Sq = 20.7%

$$t = \frac{b}{SE_b} = \frac{1.4929}{0.4870} = 3.07$$

s = 17.50

S = 17.50

estimates

This is the standard deviation of the residuals and is a measure of the average spread of the deviations from the LSRL.

Part II: Designing Experiments and Collecting Data:

Sampling Methods:

The Bad:

Voluntary sample. A voluntary sample is made up of people who decide for themselves to be in the survey. Example: Online poll

Convenience sample. A convenience sample is made up of people who are easy to reach.

Example: interview people at the mall, or in the cafeteria because it is an easy place to reach people.

The Good:

Simple random sampling. Simple random sampling refers to a method in which all possible samples of n objects are equally likely to occur.

Example: assign a number 1-100 to all members of a population of size 100. One number is selected at a time from a list of random digits or using a random number generator. The first 10 selected without repeats are the sample.

Stratified sampling. With stratified sampling, the population is divided into groups, based on some characteristic. Then, within each group, a SRS is taken. In stratified sampling, the groups are called **strata**.

Example: For a national survey we divide the population into groups or strata, based on geography - north, east, south, and west. Then, within each stratum, we might randomly select survey respondents.

Cluster sampling. With cluster sampling, every member of the population is assigned to one, and only one, group. Each group is called a cluster. A sample of clusters is chosen using a SRS. Only individuals within sampled clusters are surveyed. Example: Randomly choose high schools in the country and only survey people in those schools.

<u>Difference</u> between cluster sampling and stratified sampling. With stratified sampling, the sample includes subjects from each stratum. With cluster sampling the sample includes subjects only from sampled clusters.

Multistage sampling. With multistage sampling, we select a sample by using combinations of different sampling methods. Example: Stage 1, use cluster sampling to choose clusters from a population. Then, in Stage 2, we use simple random sampling to select a subset of subjects from each chosen cluster for the final sample.

Systematic random sampling. With systematic random sampling, we create a list of every member of the population. From the list, we randomly select the first sample element from the first *k* subjects on the population list. Thereafter, we select every *kth* subject on the list.

Example: Select every 5th person on a list of the population.

Experimental Design:

A well-designed experiment includes design features that allow researchers to eliminate extraneous variables as an explanation for the observed relationship between the independent variable(s) and the dependent variable.

Experimental Unit or Subject: The individuals on which the experiment is done. If they are people then we call them subjects **Factor:** The explanatory variables in the study

Level: The degree or value of each factor.

Treatment: The condition applied to the subjects. When there is one factor, the treatments and the levels are the same.

Control. Control refers to steps taken to reduce the effects of other variables (i.e., variables other than the independent variable and the dependent variable). These variables are called **lurking variables**.

Control involves making the experiment as similar as possible for subjects in each treatment condition. Three control strategies are control groups, placebos, and blinding.

Control group. A control group is a group that receives no treatment

Placebo. A fake or dummy treatment.

Blinding: Not telling subjects whether they receive the placebo or the treatment

Double blinding: neither the researchers or the subjects know who gets the treatment or placebo

Randomization. Randomization refers to the practice of using chance methods (random number tables, flipping a coin, etc.) to assign subjects to treatments.

Replication. Replication refers to the practice of assigning each treatment to many experimental subjects.

Bias: when a method systematically favors one outcome over another.

Types of design:

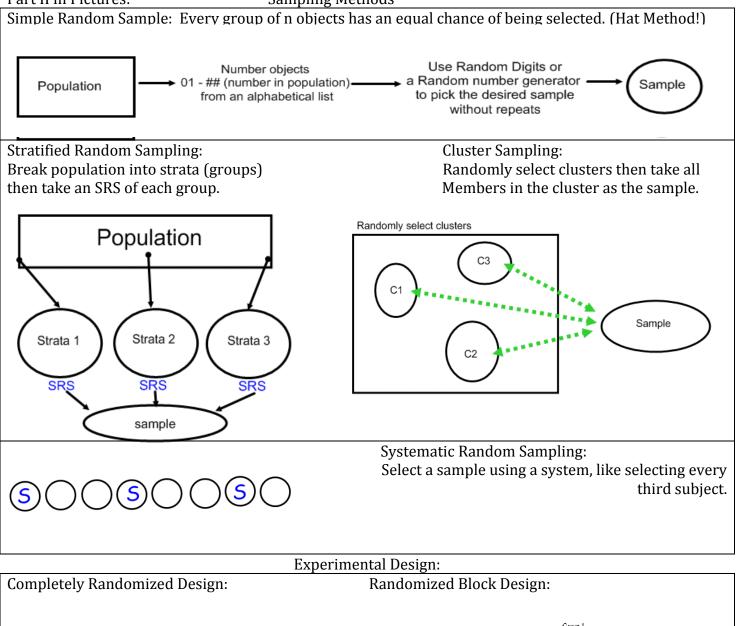
Completely randomized design With this design, subjects are randomly assigned to treatments.

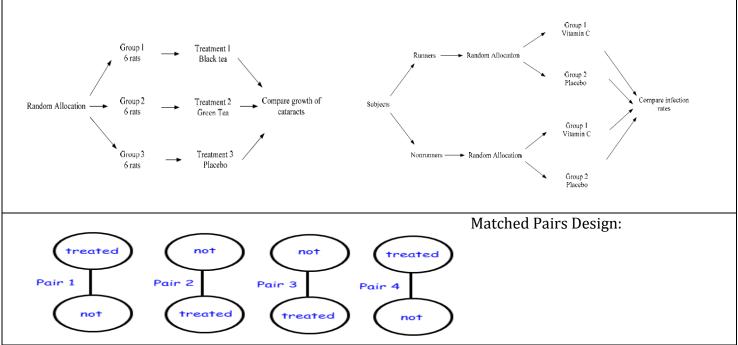
Randomized block design, the experimenter divides subjects into subgroups called **blocks**. Then, subjects within each block are randomly assigned to treatment conditions. Because this design reduces variability and potential confounding, it produces a better estimate of treatment effects.

Matched pairs design is a special case of the randomized block design. It is used when the experiment has only two treatment conditions; and subjects can be grouped into pairs, based on some blocking variable. Then, within each pair, subjects are randomly assigned to different treatments. **In some cases** you give two treatments to the same experimental unit. That unit is their own matched pair!

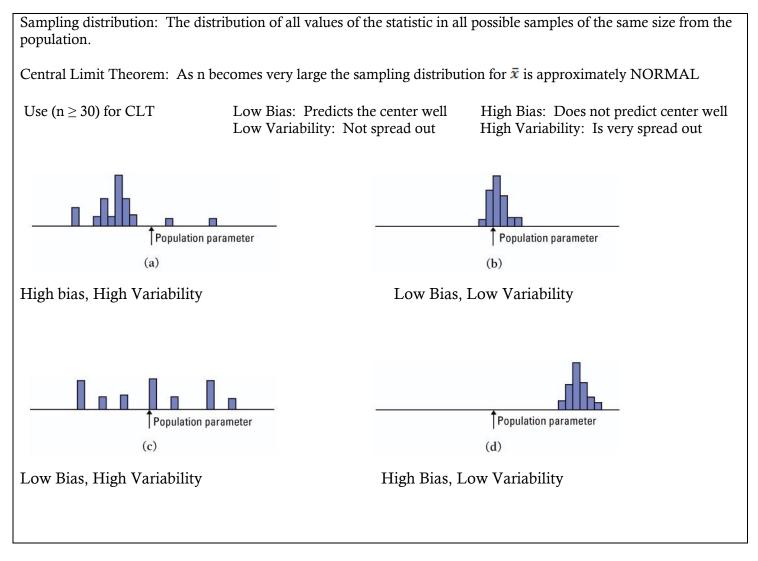
Part II in Pictures:

Sampling Methods





Part III: Probability and	Random variables.		
Counting Principle:	A and B are disjoint or	A and B are	
Trial 1: a ways	mutually exclusive if they	independent if	A B
Trial 2: b ways	have no events in	the outcome of	A D
Trial 3: c ways	common.	one does not	
The there are a x b x c ways	Roll two die: DISJOINT	affect the other.	
to do all three.	rolling a 9		
$0 \leq P(A) \leq 1$	rolling doubles	Mutually	
	Roll two die: not disjoint	Exclusive events	
	rolling a 4	CANNOT BE	
$1 - P(A) = P(A^c)$	rolling doubles	Independent	
	Toming doubles	mucpenuent	
			.4
For Conditional Drobabilit	ty use a TREE DIAGRAM	ſ	
For Conditional Flobabilit	ly use a TREE DIAGRAM	1.	P(A) = 0.3
. (0	0.7)(0.2) = 0.14 = 14%		P(B) = 0.5
0.2	, , , , , , , , , , , , , , , , , , ,		$P(A \cap B) = 0.2$
			P(A U B) = 0.3 + 0.5 - 0.2 = 0.6
0.7	0.7)(0.7) = 0.49 = 49%		P(A B) = 0.2/0.5 = 2/5
0.7			
0.1			P(B A) = 0.2 / 0.3 = 2/3
	(0.7)(0.1) = 0.07 = 7%		
	(0.3)(0.4) = 0.12 = 12%		
0.3 0.4			For Binomial Probability:
	(0, 2)(0, 5) = 0, 45 = 45 ^o		Look for x out of n trials
0.5	(0.3)(0.5) = 0.15 = 15%		1. Success or failure
			2. Fixed n
0.1			3. Independent observations
•	(0.3)(0.1) = 0.03 = 3%		4. p is the same for all observations
	Resulting		4. p is the same for an observations
	outcome		
	7. (- P.		P(X=3) Exactly 3
P(<i>B</i> <i>A</i>)	$B A \cap B$		use binompdf(n,p,3)
A			$P(X \le 3)$ at most 3
			use binomcdf(n,p,3) (Does 3,2,1,0)
P(A) $P(B' A)$	$ B' A \cap B' $		$P(X \ge 3)$ at least 3 is 1 - $P(X \le 2)$
			use 1 - binomcdf(n,p,2)
$ \langle$			
	P (4 P		Normal Approximation of Binomial:
P(A) P(B A)	$B A' \cap B$		
A'			for $np \ge 10$ and $n(1-p) \ge 10$
			the X is approx N(np, $\sqrt{np(1-p)}$)
$P(B' A^{\uparrow})$ B' $A' \cap B'$			
Discrete Random Variable	· has a countable number of	f nossible events	Geometric Probability:
	. has a countable number o	POSSIDIE EVEIIIS	
(Heads or tails, each .5)	1-1 T-1 11 · 1		Look for # trial until first success
Continuous Random Varia		interval: (EX:	1. Success or Failure
normal curve is continuous			2. X is trials until first success
Law of large numbers. As	n becomes very large $\bar{x} \rightarrow p$	u	3. Independent observations
			4. p is same for all observations
Linear Combinations:			· ·
			$P(X=n) = p(1-p)^{n-1}$
$\mu_{a+bx} = a + b\mu_x$			μ is the expected number of trails until the
$\mu_{X+Y} = \mu_x + \mu_Y$			first success or $\frac{1}{p}$
			٣
$-2 - \frac{12}{2}$			1 - m
$\sigma_{a+bx}^2 = b^2 \sigma_X^2$			$\sigma^2 = \frac{1-p}{p^2}$
			p^2
$\sigma_{X+Y}^2 = \sigma_X^2 + \sigma_Y^2$	$\sigma_{x-y}^2 = \sigma_x^2 + \sigma_y^2$		
			$P(X > n) = (1 - p)^n = 1 - P(X \le n)$
			$ D(X \setminus n) - (n)^{\mu} - D(Y \setminus n)$



See other sheets for Part IV

ART is my BFF

Type I Error: Reject the null hypothesis when it is actually True

Type II Error: Fail to reject the null hypothesis when it is False.

ESTIMATE – DO A CONFIDENCE INTERVAL

EVIDENCE - DO A TEST

Paired Procedures	Two Sample Procedures
 Must be from a matched pairs design: Sample from one population where each subject receives two treatments, and the observations are subtracted. OR Subjects are matched in pairs because they are similar in some way, each subject receives one of two treatments and the observations are subtracted 	 Two independent samples from two different populations OR Two groups from a randomized experiment (each group would receive a different treatment) Both groups may be from the same population in this case but will randomly receive a different treatment.

Major Concepts in Probability For the expected value (mean, μ_x) and the σ_x or σ_x^2 of a probability distribution use the formula sheet

For the expected value (mean, μ_X) and the σ_X of σ_X of a probability distribution use the formula sheet		
Binomial Probability	Simple Probability (and, or, not):	
Fixed Number of Trials	Finding the probability of multiple simple events.	
Probability of success is the same for all trials	Addition Rule: $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$	
Trials are independent	Multiplication Rule: $P(A \text{ and } B) = P(A)P(B A)$	
If X is B(n,p) then (ON FORMULA SHEET)	Mutually Exclusive events CANNOT be independent	
Mean $\mu_X = np$	A and B are independent if the outcome of one does not affect	
Standard Deviation $\sigma_x = \sqrt{np(1-p)}$ For Binomial probability use $P(X = k) = \binom{n}{k} p^k (1-p)^{n-k}$ or use:	the other. A and B are disjoint or mutually exclusive if they have no	
$\sum_{n=1}^{\infty} \sum_{i=1}^{n} \frac{1}{1} \frac{1}$	events in common.	
For Binomial probability use $P(X = k) = {n \choose k} p^k (1-p)^{n-k}$ or use:	Roll two die: DISJOINT	
Exactly: $P(X = x) = binompdf(n, p, x)$	rolling a 9	
Exactly: $f(X - x) = 0$ in only $f(x, y)$	rolling doubles	
At Most: $P(X \le x) = binomcdf(n, p, x)$		
	Roll two die: NOT disjoint	
At least: $P(X \ge x) = 1$ - binomcdf(n, p, x-1)	rolling a 4	
	rolling doubles	
More than: $P(X > x) = 1$ - binomcdf(n, p, x)		
	Independent: $P(B) = P(B A)$	
Less Than: $P(X < x) = binomcdf(n, p, x-1)$	Mutually Exclusive: P(A and B) = 0	
You may use the normal approximation of the binomial		
distribution when $np \ge 10$ and $n(1-p) \ge 10$. Use then mean and		
standard deviation of the binomial situation to find the Z score.		
Geometric Probability	Conditional Probability	
You are interested in the amount of trials it takes UNTIL	Finding the probability of an event given that another even	
you achieve a success.	has already occurred.	
Probability of success is the same for each trial	Conditional Probability: $P(B A) = \frac{P(A \cap B)}{P(A)}$	
Trials are independent	$\frac{P(A)}{P(A)} = \frac{P(A)}{P(A)}$	
	Use a two way table or a Tree Diagram for Conditional	
Use simple probability rules for Geometric Probabilities.	Problems.	
	Events are Independent if $P(B A) = P(B)$	
$P(X=n) = p(1-p)^{n-1}$ $P(X > n) = (1-p)^n = 1 - P(X \le n)$		
$\mu_{\rm X}$ is the expected number of trails until the first success or $\frac{1}{p}$		
p p		
Normal Pro		
For a single observation from a normal population	For the mean of a random sample of size n from a population.	
	When n > 30 the sampling distribution of the sample mean \bar{x}	
$P(X > y) = P(z > x - \mu)$ $P(X < y) = P(z < x - \mu)$	is approximately Normal with:	
$P(X > x) = P(z > \frac{x - \mu}{\sigma}) \qquad P(X < x) = P(z < \frac{x - \mu}{\sigma})$	$\mu_{\overline{\chi}} = \mu$	
Ŭ Ŭ		
	$\sigma = \sigma$	
	$\sigma_{\overline{X}} = \frac{\sigma}{\sqrt{n}}$	
6.2	If $n < 30$ then the population should be Normally distributed	
	to begin with to use the z-distribution.	
	$P(\overline{X} > x) = P(z > \frac{x - \mu}{z})$ $P(\overline{X} < x) = P(z < \frac{x - \mu}{z})$	
	$P(\overline{X} > x) = P(z > \frac{x - \mu}{\sigma/n}) \qquad P(\overline{X} < x) = P(z < \frac{x - \mu}{\sigma/n})$	
To find $P(x < X < y)$ Find two Z scores and subtract the	$/\sqrt{n}$	
probabilities (upper – lower)	To find $P(x < X < y)$ Find two Z scores and subtract the	
	probabilities (upper – lower)	
Use the table to find the probability or use	Use the table to find the probability or use	
normalcdf(min,max,0,1) after finding the z-score	normalcdf(min,max,0,1) after finding the z-score	

Binomial Probability	Simple Probability (and, or, not):
Mr. K is shooting three point jump shots. Mr. K has a career shooting percentage of 80%. Mr. K is going to shoot 30 three pointers during a practice session. X: number of threes made, X is B(30, 0.6) $\mu_X = np = 30(.6) = 18$ $\sigma_X = \sqrt{np(1-p)} = \sqrt{30(.60)(.40)} = 2.683$	
The probability that Mr. K makes exactly 20 is: P(X = 20) = binompdf(30, 0.6, 20) = 0.1152 The probability that Mr. K makes at most 20 is: $P(X \le 20) = binomcdf(30, 0.6, 20) = 0.8237$ The probability the Mr. K makes at least 20 is: $P(X \ge 20) = 1 - binomcdf(30, 0.6, 19) = 1 - 0.7085 = 0.2915$	P(A) = 0.3 P(B) = 0.5 $P(A \cap B) = 0.2$ $P(A \cup B) = 0.3 + 0.5 - 0.2 = 0.6$ $P(A \mid B) = 0.2/0.5 = 2/5$ $P(B \mid A) = 0.2/0.3 = 2/3$ $P(A^{\circ}) = 1 - 0.3 = 0.7$
Geometric Probability	Conditional Probability with a Tree Diagram
The population of overweight manatees is known to be 40% You select a random Manatee and weigh it, and then you repeat the selection until one is overweight. Find the probability that the fifth manatee you choose is	Of adult users of the Internet: 29% are 18-29 47% are 30-49 24% are over 50 47% of the 18-29 group chat 21% of the 30-49 group chat
overweight. $P(X = 5) = (notover)^4 (over) = (0.60)^4 (0.40) = .05184$	7% of the 50 and over group chat. Find the probability that a randomly selected adult chats
Find the probability that it takes more than five attempts to find an overweight manatee.	0.53 <i>C^c</i> 0.1537 0.29 0.21 <i>C</i> 0.0987*
$P(X > 5) = (notoverweight)^5 = (0.60)^5 = 0.07776$	Internet 0.47 A2 CLT 0 COOP
How many manatees would you expect to choose before you found one to be overweight?	$\begin{array}{cccc} 0.79 & & C^c & & 0.3713 \\ \end{array}$ $\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\mu_x = \frac{1}{p} = \frac{1}{0.4} = 2.5$	0.93 <i>C^c</i> 0.2232
Normal Probability	Conditional Probability with a two way table:
The weight of manatees follows a normal distribution with a mean weight of 800 pounds and a standard deviation of 120 pounds.	Table 6.1 Grades awarded at a university, by school Grade Level A B Below B Total
Find the probability that a randomly selected Manatee weighs more than 1000 pounds: X is N(800,120)	Liberal Arts2,1421,8902,2686,300Engineering and Physical Sciences3684328001,600Health and Human Services8826305882,100Total3,3922,9523,65610,000
$P(X > 1000) = P(z > \frac{1000 - 800}{120}) = P(z > 1.67) = 0.0475$	P(A grade liberal arts course) = 2142 / 6300
Find the probability that a random sample of 50 manatees has a mean weight more than 1000 pounds:	P(Liberal arts course A Grade) = $2142 / 3392$
$P(\overline{X} > 1000) = P(z > \frac{1000 - 800}{120/\sqrt{50}}) = P(z > 11.79) \approx 0$	P(B Grade Engineering and PS) = 432 / 1600 P(Engineering and PS B Grade) = 432 / 2952
Even if you did not know the population was normal you could use CLT and assume the sampling distribution is approximately normal.	1 (Engineering and 1.5 D (Ender) = 4.32 / 2.332

Mutually Exclusive vs. Independence

You just heard that Dan and Annie who have been a couple for three years broke up. This presents a problem, because you're having a big party at your house this Friday night and you have invited them both. Now you're afraid there might be an ugly scene if they both show up. When you see Annie, you talk to her about the issue, asking her if she remembers about your party. She assures you she's coming. You say that Dan is invited, too, and you wait for her reaction. If she says, "That jerk! If he shows up I'm not coming. I want nothing to do with him!", they're **mutually exclusive**. If she says, "Whatever. Let him come, or not. He's nothing to me now.", they're **independent**.

Mutually Exclusive and Independence are two very different ideas

Mutually Exclusive (disjoint):	Independence:
$\frac{P(A \text{ and } B) = 0}{P(A \text{ and } B) = 0}$	$\frac{P(B) = P(B A)}{P(B A)}$
Events A and B are mutually exclusive if they have no	Events A and B are independent if knowing one outcome
outcomes in common.	does not change the probability of the other.
That is A and B cannot happen at the same time.	That is knowing A does not change the probability of B.
Example of mutually exclusive (disjoint) :	Examples of independent events:
A: roll an odd on a die	A: draw an ace
B: roll an even on a die	B: draw a spade
Odd and even share no outcomes	$P(Spade) = \frac{13}{52} = \frac{1}{4}$
P(odd and even) = 0	$P(\text{Spade} \mid \text{Ace}) = 1/4$
Therefore, they are mutually exclusive.	Knowing that the drawn card is an ace does not change the
	probability of drawing a spade
Example of <u>not</u> mutually exclusive (joint) :	
A: draw a king	Examples that are dependent (not independent):
B: draw a face card	A: roll a number greater than 3
	B: roll an even
King and face card do share outcomes . All of the kings	
are face cards.	P(even) = 3/6 = 1/2
P(king and face card) = $4/52$	P(even greater than 3) = $2/3$
Therefore, they are not mutually exclusive.	Knowing the number is greater than three changes the
	probability of rolling an even number.

Mutually Exclusive events	Independent events cannot be	Dependent Events may or
cannot be independent	Mutually Exclusive	may not be mutually exclusive
-		Dependent and mutually exclusive
Mutually exclusive and	Independent and not mutually	A: draw a queen
dependent	exclusive	B: draw a king
-		Knowing it is a queen changes the probability of
A: Roll an even	A: draw a black card	it being a king and they do not share outcomes.
B: Roll an odd	B: draw a king	
		Dependent and not mutually exclusive
They share no outcomes and	Knowing it is a black card does	A: Face Card
knowing that it is odd changes	not change the probability of it	B: King
the probability of it being even.	being a king and they do share	Knowing it is a face card changes the probability
	outcomes.	of it being a king and they do share outcomes.

If events are mutually exclusive then:	If events are independent then:
P(A or B) = P(A) + P(B)	P(A and B) = P(A)P(B)
If events are not mutually exclusive use the general rule:	If events are not independent then use the general rule:
P(A or B) = P(A) + P(B) - P(A and B)	P(A and B) = P(A)P(B A)

Interpretation for a Confidence Interval:

I am C% confident that the true parameter (mean μ or proportion p) lies between # and #. INTERPRET IN CONTEXT!!

<u>Interpretation of C% Confident:</u> Using my method, If I sampled over and over again, C% of my intervals would contain the true parameter (mean μ or proportion p).

NOT: The parameter lies in my interval C% of the time. It either does or does not!!

If $p < \alpha$ I reject the null hypothesis H_0 and I have sufficient/strong evidence to support the alternative hypothesis H_a

INTERPRET IN CONTEXT in terms of the alternative.

If $p > \alpha$ I fail to reject the null hypothesis H₀ and I have insufficient/poor evidence to support the alternative hypothesis H_a

INTERPRET IN CONTEXT in terms of the alternative.

Evidence Against H _o	
P-Value	
"Some"	0.05 < P-Value < 0.10
"Moderate or Good"	0.01 < P-Value < 0.05
"Strong"	P-Value < 0.01

Interpretation of a p-value:

The probability, assuming the null hypothesis is true, that an observed outcome would be as extreme or more extreme than what was actually observed.

Duality: Confidence intervals and significance tests.

If the hypothesized parameter lies outside the C% confidence interval for the parameter I can REJECT $\rm H_0$

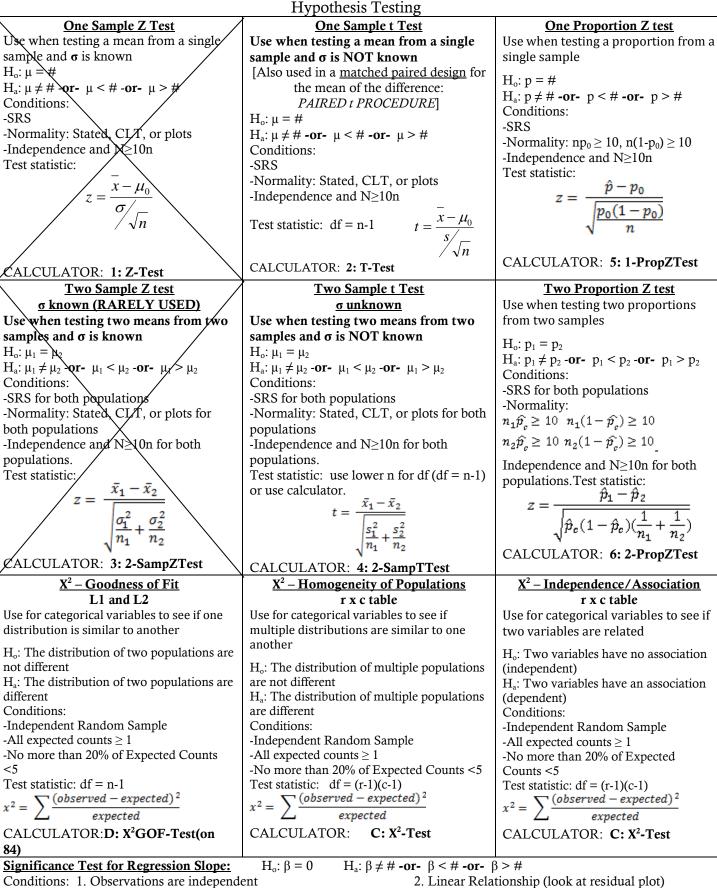
If the hypothesized parameter lies inside the C% confidence interval for the parameter I FAIL TO REJECT $\rm H_0$

Power of test:

The probability that at a fixed level α test will reject the null hypothesis when and alternative value is true.

	Confidence Intervals	
One Sample Z Interval	One Sample t Interval	One Proportion Z Interval
Use when estimating a single	Use when estimating a single mean	Use when estimating a single
population mean and σ is known	and σ is NOT known	proportion
Conditions:	[Also used in a <u>matched paired design</u>	Conditions:
-SRS	for the mean of the difference:	-SRS
-Normality: CLT, stated /or plots	PAIRED t PROCEDURE]	-Normality: $n\hat{p} \ge 10, \ n(1-\hat{p}) \ge 10$
-Independence and N≥∕10n	Conditions:	
Interval:	-SRS	-Independence and N≥10n
$-\sqrt{\sigma}$	-Normality: CLT, stated, or plots	Interval:
$x \pm z \sqrt{-\pi}$	-Independence and N≥10n	$\hat{n} + \hat{n}(1-\hat{n})$
$\frac{1}{x \pm z} \frac{\sigma}{\sqrt{n}}$	Interval:	$\hat{p} \pm z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$
	- * S	n
	$\overline{x} \pm t^* \frac{s}{\sqrt{n}}$	
	\sqrt{n}	
	df = n-1	
CALCULATOR:	CALCULATOR:	
7:/Z-Interval	8: T-Interval	CALCULATOR:
		A: 1-PropZInt
Two Sample Z Interval	Two Sample t Interval	Two Proportion Z Interval
<u>σ known (RARELY USED)</u>	<u> </u>	Use when estimating the difference
Use when estimating the	Use when estimating the difference	between two population proportions.
difference between two	between two population means and σ	Conditions:
population means and σ is known	is NOT known	-SRS for both populations
Conditions:	Conditions:	-Normality:
-SRS for both populations	-SRS for both populations	$n_1 \hat{p}_1 \ge 10 \ n_1 (1 - \hat{p}_1) \ge 10$
-Normality: CLT, stated, or plots	-Normality: CLT, stated, or plots for	$n_1\hat{p}_1 \ge 10$ $n_1(1 - \hat{p}_1) \ge 10$ $n_2\hat{p}_2 \ge 10$ $n_2(1 - \hat{p}_2) \ge 10$
for -both populations	both populations	
-Independence and N≥10n for	-Independence and N≥10n for both	-Independence and N≥10n for both
both populations.	populations.	populations.
Interval:	Interval:	Interval:
$\sqrt{\frac{1}{2}}$	$\int g^2 g^2$	$(\hat{p}_1 - \hat{p}_2) \pm z^* \sqrt{\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2}}$
$\left(\frac{-}{x_1} - \frac{-}{x_2} \right) + \frac{-}{2} + \frac{-}$	$(\bar{x}_1 - \bar{x}_2) \pm t^* \sqrt{\frac{s_1^2}{1} + \frac{s_2^2}{2}}$	$(p_1 - p_2) \pm z$ $\sqrt{n_1} + \frac{n_2}{n_2}$
		V I Z
$\bigvee n_1 \setminus n_2$	$n_1 n_2$	
	Use lower n for df (df = $n-1$) or use	
	calculator	
CALCULATOR:	CALCULATOR:	CALCULATOR:
9: 2-SampZInt	0: 2-SampTInt	B: 2-PropZInt
Y	Confidence interval for Regression Slop	
Use when estimating the slope of the		
Conditions:	0	
1. Observations are independent		
2. Linear Relationship (look at resid	ual plot)	
3. Standard deviation of y is the sam		
	· · · · · · · · · · · · · · · · · · ·	
4. y varies normally (look at histogr		
4. y varies normally (look at histogr Interval:		
Interval:		

df = n - 2CALCULATOR:LinRegTIntUse technology readout or calculator for this confidence interval.



Conditions: 1. Observations are independent 2. Linear Relationship (look at residual plot) 3. Standard deviation of y is the same(look at residual plot) 4. y varies normally (look at histogram of residuals) CALCULATOR: LinRegTTest Use technology readout or the calculator for this significance test $t = \frac{b}{SE}$ df = n-2

Notation and Interpretations

IQR	Inner Quartile Range
x	Mean of a sample
μ	Mean of a population
s	Standard deviation of a sample
σ	Standard deviation of a population
p	Sample proportion
p	Population proportion
$\frac{r}{s^2}$	Variance of a sample
σ^2	Variance of a population
М	Median
Σ	Summation
Q1	First Quartile
Q ₃	Third Quartile
Z	Standardized value – z test statistic
Z	Critical value for the standard normal distribution
t*	Test statistic for a t test
t [°]	Critical value for the t-distribution
N(μ, σ)	Notation for the normal distribution with mean and standard deviation
r r^2	Correlation coefficient – strength of linear relationship Coefficient of determination – measure of fit of the model to the data
$\hat{v} = a + bx$	Equation for the Least Squares Regression Line
/	
a b	y-intercept of the LSRL
$(\overline{x}, \overline{y})$	Slope of the LSRL Point the LSRL passes through
$y = ax^b$	Power model
y = ax $y = ab^x$	Exponential model
SRS	Simple Random Sample
S	Sample Space
P(A)	The probability of event A
A ^c	A complement
P(B A)	Probability of B given A
\bigcap	Intersection (And)
U	Union (Or)
Х	Random Variable
μ_X	Mean of a random variable
σχ	Standard deviation of a random variable
σ_X^2	Variance of a random variable
B(n,p)	Binomial Distribution with observations and probability of success
$\binom{n}{k}$	Combination n taking k
pdf	Probability distribution function
cdf	Cumulative distribution function
n N	Sample size Population size
CLT	Central Limit Theorem
$\mu_{\bar{x}}$	Mean of a sampling distribution
	Standard deviation of a sampling distribution
σ _x	
df SE	Degrees of freedom Standard error
H ₀	Standard error Null hypothesis-statement of no change
H ₀ H _a	Alternative hypothesis- statement of change
p-value	Probability (assuming H_0 is true) of observing a result as large or larger than that observed
α	Significance level of a test. P(Type I) or the y-intercept of the true LSRL
β	P(Type II) or the true slope of the LSRL
χ^2	Chi-square test statistic

z-score (z)	The number of standard deviations an observation is above/below the mean
slope (b)	The change in predicted y for every unit increase on x
y-intercept (a)	Predicted y when x is zero
r (correlation coefficient)	strength of linear relationship. (Strong/moderate/weak) (Positive/Negative) linear relationship between y and x.
r ² (coefficient of determination)	percent of variation in y explained by the LSRL of y on x.
variance (σ^2 or s^2)	average squared deviation from the mean
standard deviation (σ or s)	measure of variation of the data points from the mean
Confidence Interval (#,#)	I am C% confident that the true parameter (mean μ or proportion p) lies between # and #.
C % Confidence (Confidence level)	Using my method, If I sampled repeatedly, C% of my intervals would contain the true parameter (mean μ or proportion p).
$p < \alpha$	Since $p < \alpha$ I reject the null hypothesis H ₀ and I have sufficient/strong evidence to conclude the alternative hypothesis Ha
$p > \alpha$	Since $p > \alpha$ I fail to reject the null hypothesis H ₀ and I have do not have sufficient evidence to support the alternative hypothesis Ha
p-value	The probability, assuming the null hypothesis is true, that an observed outcome would be as or more extreme than what was actually observed.
Duality-Outside Interval Two sided test	If the hypothesized parameter lies outside the $(1 - \alpha)$ % confidence interval for the parameter I can REJECT H ₀ for a two sided test.
Duality-Inside Interval Two sided test	If the hypothesized parameter lies inside the $(1 - \alpha)$ % confidence interval for the parameter I FAIL TO REJECT H ₀ for a two sided test.
Power of the test	The probability that a fixed level test will reject the null hypothesis when an alternative value is true
standard error (SE) in general	Estimates the variability in the sampling distribution of the sample statistic.
standard deviation of the residuals (s from regression)	A typical amount of variability of the vertical distances from the observed points to the LSRL
standard error of the slope of the LSRL (SE _b)	This is the standard deviation of the estimated slope. This value estimates the variability in the sampling distribution of the estimated slope.

